# Polydispersity Effects in the System Poly(ethylene glycol) + Dextran + Water 

Johann Gaube,' Ralf Höchemer, Bernhard Keil, and Andreas Pfennig<br>Institut für Chemische Technologie, Technische Hochschule Darmstadt, Petersenstrasse 20, D-6100 Darmstadt, Germany


#### Abstract

Tie lines in the system poly(ethylene glycol) (PEG) + dextran + water have been measured at $20^{\circ} \mathrm{C}$. The apparent polydispersity of PEG was varied by mixing two essentially monodisperse PEG fractions in different ratios. The overall phase composition for a given tie line was changed to obtain phase ratios different from unity. The concentrations and molecular-weight distributions of all polymers in the coexisting liquid phases were determined using size-exclusion chromatography (SEC). The results are compared to those of systems containing monodisperse PEG with different molecular weights.


## Introduction

Aqueous polymer-polymer two-phase systems become increasingly attractive for the separation of complex mixtures of biomolecules (1). To design an industrial separation process, theoretical models for the prediction of the phase behavior are necessary. The development of such models requires accurate and reliable thermodynamic information on the phase compositions in the coexisting phases and on the polydispersity effects in the system. The polydispersity of the phase-forming polymer has a strong influence on some thermodynamic properties, especially the liquid-liquid equilibrium (2). The polymers in the coexisting phases have different molecular-weight distributions. Also the phase ratio for a given tie line has an influence on the coexistence curve. To describe these effects in modeling, the molecular-weight distribution has to be taken into account (3). For dextran the molecular-weight distributions in the top and bottom phases have been explored in a previous paper (4). In this study the polydisperse effects of PEG are investigated. Since the commercially available PEG is essentially monodisperse, the polydispersity was simulated by mixing two PEG's with different molecular weights.

## Experimental Section

Materials. The components were used in the highest purity commercially available without further purification. PEG 600, 1550, and 3000 were supplied by the Hüls AG, Marl. Dextran 500000 was purchased from Pfeifer \& Langen, Dormagen. The water was triple distilled. The number- and mass-average molecular weights of the used PEG's, determined by size-exclusion chromatography, are presented in Table I. The dextran molecular-weight standards were supplied by Pharmacosmos, Denmark, the PEG standards by Polymer Laboratories, U.K.

Analytical Methods. The PEG and dextran concentrations in each phase were measured by size-exclusion chromatography (SEC). The chromatographic equipment consists of a degasser (ERC-3312), a HPLC pump (ERC-64), a pulsation damper, a rotary valve (Rheodyne 7125), three 30cm SEC columns in series (TSK G6000PWXL, PSS HEMA 1000, TSK G3000PWXL) and a refractive-index detector (ERC-7512). The columns and the rotary valve with sample loop were placed in a column thermostat (Spark Holland 99). The refractive-index detector and the columns were thermostated at $35^{\circ} \mathrm{C}$. The eluent was distilled water, purified with a Millipore Milli-Q-System, to which 200 ppm sodium

Table I. Average Molecular Weights of Stock Solutions ${ }^{A}$

|  | lot no. | $M_{\mathrm{n}} /\left(\mathrm{g} \mathrm{mol}^{-1}\right)$ | $M_{\mathrm{w}} /\left(\mathrm{g} \mathrm{mol}^{-1}\right)$ |
| :--- | :---: | ---: | :---: |
| PEG 600 | P.2 | 585 | 600 |
| PEG 1550 | P.8 | 1464 | 1485 |
| PEG 3000 | P.2 | 2810 | 3026 |
| PEGG 600/3000 $\left(M_{\mathrm{n}}\right)$ |  | 1480 | 2365 |
| PEG 600/3000 $\left(M_{\mathrm{w}}\right)$ |  | 862 | 1560 |
| dextran PL 500 VC | 5008622 | 109292 | 493109 |

[^0]azide was added (5). The pumping rate of the HPLC pump was $1 \mathrm{~cm}^{3} / \mathrm{min}$. The calibration method was the same as that applied by Connemann et al. (4).

Phase Systems. Six aqueous two-phase systems containing various PEG fractions, dextran 500000 , and water have been investigated. The generation and separation of the phase systems follow the same procedure as that described in ref 4. For identification the systems are marked with letters from A to G (Tables II and III).

Table II presents the tie-line data and average molecular weights of the systems $A$ and $B$ containing the PEG fractions 600 and 1550 , respectively. Additionally a third ternary system prepared with PEG 3000 (system C) is included. The data for this system have been reported previously (4).

To explore the polydispersity effects of PEG, phase systems were generated using PEG stock solutions mixed from PEG 600 and PEG 3000. These two PEG fractions were chosen because they can be completely separated with SEC. The mixtures of PEG fractions can be adjusted to have a numberaverage or mass-average molecular weight close to that of PEG 1550. This could be achieved by mixing PEG 600 and PEG 3000 in the ratio of $w_{\text {PEG } 600} / w_{\text {PEG } 3000}=0.348$ to obtain the polydisperse PEG with the number-average molecular weight close to $1550 \mathrm{~g} \mathrm{~mol}^{-1}$ and $w_{\text {PEG } 600} / w_{\text {PEG } 3000}=1.525$ for that with the mass-average molecular weight close to 1550 g $\mathrm{mol}^{-1}$. The exact molecular weights of the corresponding stock solutions are also given in Table I. The stock solution with an $M_{\mathrm{n}}$ close to that of PEG 1550 (index $M_{n}$ ) was used to prepare systems D, F, and G, the one with $M_{w}$ similar to that of PEG 1550 (index $M_{w}$ ) for system E.

The systems D and E were generated with phase ratios near unity. For the systems $F$ and $G$ the overall composition was chosen close to the dextran-rich and PEG-rich ends of the tie lines, respectively. This experiments should reveal the effect of the phase ratio on the phase compositions and the molecular-weight distributions of both polymers for a

Table II. Determination of the Tie Lines for the Ternary Systems PEG + Dextran + Water and Average Molecular Weights of Dextran

| index | composition/(mass \%) |  |  |  |  |  | tie-line length/( $g / g$ ) | dextran average molecular weight/(g mol ${ }^{-1}$ ) |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | total |  | top phase |  | bottom phase |  |  | top phase |  | bottom phase |  |
|  | $\overline{\text { PEG }}$ | dextran | PEG | dextran | PEG | dextran |  | $M_{\mathrm{n}}$ | $M_{\text {w }}$ | $M_{\text {n }}$ | $M_{\text {w }}$ |
| System A: PEG 600 + Dextran 500000 + Water |  |  |  |  |  |  |  |  |  |  |  |
| 1 | 14.84 | 10.73 | 19.09 | 3.34 | 13.32 | 15.10 | 10.19 | 67000 | 119748 | 113744 | 514158 |
| 2 | 16.84 | 11.83 | 22.55 | 1.04 | 11.06 | 23.04 | 19.06 | 45665 | 71326 | 107073 | 451683 |
| 3 | 17.37 | 12.48 | 23.84 | 0.75 | 10.29 | 26.22 | 22.07 | 38330 | 68395 | 101464 | 447542 |
| 4 | 18.79 | 13.53 | 26.06 | 0.30 | 8.62 | 31.67 | 27.22 | 31698 | 57808 | 102588 | 448402 |
| 5 | 19.66 | 14.71 | 27.64 | 0.06 | 8.06 | 34.85 | 30.21 | 30385 | 34539 | 100114 | 430362 |
| 6 | 20.29 | 15.54 | 29.21 | 0.07 | 7.75 | 37.45 | 32.49 | 22352 | 30570 | 100118 | 446267 |
| System B: PEG 1550 + Dextran 500000 + Water |  |  |  |  |  |  |  |  |  |  |  |
| 7 | 9.05 | 8.08 | 11.15 | 3.18 | 7.28 | 11.93 | 7.59 | 77794 | 138494 | 129136 | 486174 |
| 8 | 9.06 | 8.49 | 11.69 | 2.64 | 6.94 | 13.29 | 9.24 | 70185 | 115761 | 118567 | 462465 |
| 9 | 9.58 | 10.09 | 13.86 | 0.88 | 5.20 | 19.34 | 16.00 | 50536 | 70517 | 119028 | 441921 |
| 10 | 9.85 | 11.80 | 15.47 | 0.41 | 4.25 | 23.23 | 19.76 | 37870 | 49985 | 101766 | 393164 |
| 11 | 8.95 | 14.95 | 16.19 | 0.31 | 3.80 | 25.10 | 21.47 | 34212 | 42852 | 106709 | 399612 |
| 12 | 11.08 | 13.99 | 18.16 | 0.14 | 3.07 | 29.48 | 25.41 | 27860 | 34021 | 105530 | 400696 |

Table III. Determination of the Tie Lines for the Quarternary Systems PEG 600/3000 + Dextran $500 \mathbf{0 0 0}+$ Water and Average Molecular Weights of PEG and Dextran

| index | composition/(mass \%) |  |  |  |  |  |  |  |  | tie-line length/ (g/g) | average molecular weight/(g mol${ }^{-1}$ ) |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | total |  |  | top phase |  |  | bottom phase |  |  |  |  |  | phase |  |  |  | om phase |  |
|  | PEG | PEG |  | PEG | PEG |  | PEG | PEG |  |  | PEG |  | dextran |  | PEG |  | dextran |  |
|  | 600 | 3000 | dextran | 600 | 3000 | dextran | 600 | 3000 | dextran |  | $M_{n}$ | $M_{\text {w }}$ | $M_{n}$ | $M_{\text {w }}$ | $M_{n}$ | $M_{w}$ | $M_{n}$ | $M_{\text {w }}$ |
| System D with PEG 600/3000 ( $M_{n}$ ) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 13 | 2.03 | 6.75 | 6.31 | 8.85 | 2.37 | 1.01 | 2.61 | 1.61 | 16.06 | 13.04 | 1549 | 2411 | 59841 | 115909 | 1090 | 1955 | 123630 | 511782 |
| 14 | 2.20 | 7.32 | 7.38 | 10.28 | 2.72 | 0.58 | 1.91 | 1.55 | 19.77 | 16.62 | 1369 | 2372 | 50205 | 134610 | 937 | 1775 | 115613 | 471896 |
| 15 | 2.36 | 7.85 | 8.93 | 11.60 | 2.90 | 0.18 | 1.32 | 1.54 | 23.43 | 20.14 | 1469 | 2414 | 34081 | 139665 | 826 | 1550 | 112915 | 477048 |
| 16 | 2.50 | 8.31 | 10.38 | 12.93 | 3.21 | 0.05 | 1.07 | 1.56 | 26.37 | 22.80 | 1487 | 2414 | 34189 | 39976 | 774 | 1440 | 111116 | 480602 |
| 17 | 2.61 | 8.69 | 11.75 | 14.12 | 3.52 | 0.10 | 0.84 | 1.57 | 28.81 | 24.88 | 1460 | 2409 | 37775 | 68868 | 667 | 1309 | 109415 | 468984 |
| 18 | 2.70 | 8.98 | 13.24 | 15.27 | 3.69 | 0.08 | 0.69 | 1.53 | 31.02 | 26.82 | 1502 | 2423 | 66268 | 123180 | 683 | 1228 | 108017 | 460696 |
| System E with PEG 600/3000 ( $M_{\mathrm{w}}$ ) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 19 | 4.16 | 4.88 | 7.81 | 5.51 | 5.74 | 3.34 | 4.60 | 3.33 | 10.16 | 5.92 | 906 | 1653 | 71440 | 140824 | 809 | 1463 | 111000 | 479326 |
| 20 | 4.38 | 5.15 | 9.08 | 6.35 | 7.16 | 1.25 | 3.73 | 2.70 | 15.49 | 12.34 | 936 | 1712 | 49253 | 75268 | 733 | 1267 | 105901 | 441200 |
| 21 | 5.16 | 6.05 | 10.53 | 7.85 | 8.85 | 0.36 | 2.96 | 2.14 | 21.89 | 18.66 | 935 | 1703 | 35478 | 41990 | 640 | 993 | 101988 | 416771 |
| 22 | 3.60 | 4.23 | 10.65 | 7.47 | 11.69 | 0.09 | 2.41 | 1.74 | 28.03 | 24.21 | 1068 | 1886 | 28927 | 36634 | 621 | 953 | 99362 | 428621 |
| System F (Dextran-Rich) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 24 | 3.06 | 0.91 | 17.77 | 1.60 | 10.58 | 0.38 | 1.01 | 1.91 | 19.80 | 16.82 | 1901 | 2609 | 41064 | 57452 | 1214 | 2072 | 110979 | 478258 |
| 25 | 2.65 | 0.79 | 22.28 | 1.70 | 12.82 | 0.11 | 0.78 | 1.17 | 24.63 | 21.24 | 1977 | 2630 | 37856 | 59561 | 1089 | 1906 | 110594 | 473940 |
| 26 | 2.52 | 0.75 | 25.18 | 1.73 | 14.70 | 0.25 | 0.79 | 0.84 | 27.91 | 23.98 | 2063 | 2694 | 23308 | 32140 | 984 | 1756 | 110429 | 478511 |
| System G (PEG-Rich) |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| 28 | 9.40 | 2.81 | 1.91 | 3.01 | 9.96 | 0.31 | 1.84 | 2.07 | 18.94 | 16.13 | 1482 | 2354 | 47534 | 67142 | 991 | 1782 | 138075 | 542165 |
| 29 | 11.33 | 3.38 | 1.60 | 3.55 | 11.80 | 0.13 | 1.92 | 1.03 | 24.71 | 21.29 | 1503 | 2379 | 38062 | 56423 | 783 | 1351 | 122639 | 484896 |
| 30 | 11.84 | 3.54 | 1.33 | 3.68 | 12.22 | 0.09 | 1.92 | 1.05 | 25.09 | 21.66 | 1490 | 2364 | 41095 | 55018 | 764 | 1351 | 122098 | 503323 |
| 31 | 12.91 | 3.86 | 1.21 | 3.98 | 13.23 | 0.03 | 2.00 | 0.89 | 26.67 | 23.09 | 1484 | 2356 | 35051 | 39940 | 794 | 1273 | 117152 | 492948 |

given tie line. The tie-line data and average molecular weights for these quarternary systems are given in Table III.

## Results and Discussion

The molecular weight as well as the molecular-weight distribution of the phase-forming polymers have a considerable effect on the miscibility of the phase system. In Figure 1 the influence of the number- and mass-average molecular weights on the phase behavior is demonstrated by comparing the binodal curves of the various phase systems with a phase ratio close to unity. This figure illustrates that the miscibility of the components increases with decreasing PEG molecular weight. The systems $B$ and $E$ have miscibility gaps of similar size. The binodal curve of system $D$ lies between the binodal curves of systems B and C. This indicates that it is the massaverage molecular weight which approximately determines the size of the region of immiscibility. Comparing the trend of the binodal curves of systems $D$ and $E$ at the dextran-rich end with those containing monodisperse PEG, it can be seen that the polydispersity of a polymer increases its solubility in the phase which is poor in this polymer.


Figure 1. Tie lines of systems A-E at $20^{\circ} \mathrm{C}$.
Figure 2 presents chromatograms corresponding to the coexisting phases of tie line 15 to illustrate the different amounts of the three polymer fractions in these phases. From this figure it is apparent that the high-molecular-weight PEG


Figure 2. Chromatograms corresponding to tie line 15: (- . -) top phase; ( - ) bottom phase.


Figure 3. Tie lines of systems D, F, and G at $20^{\circ} \mathrm{C}$ : ( $\square, \nabla$, $X$ ) total composition; $(\square, \nabla, \boxed{Z})$ composition of corresponding phases.
fraction remains preferably in the PEG-rich top phase while the small PEG molecules are driven into the dextran-rich bottom phase.

Figure 3 demonstrates the polydispersity effects which result from a phase ratio different from unity. For better readability, only every second tie line is shown. In the case of system $F$ with the highest overall ratio of dextran/PEG the lowest miscibility of PEG in the dextran-rich bottom phase is bound. Furthermore, the tie lines of these system are longer than all others. With decreasing overall ratio of dextran/ PEG the composition in the bottom phase is shifted to a higher dextran and a lower PEG concentration. For system $G$ with a PEG-rich overall composition this trend is oppositely but only weakly affected. No effect of the phase ratio on the phase composition in the top phase was detectable for the system investigated. The effect may be smaller than the experimental accuracy.

To investigate the influence of the phase ratio on the molecular-weight distributions of dextran and PEG in the coexisting phases, the distributions corresponding to tie lines 23 (dextran rich) and 27 (PEG rich) are compared to that of tie line 13 in Figures 4 and 5.

Figure 4 demonstrates that preferably the low-molecularweight dextran molecules dissolve in the top phase. In the case of a dextran-rich overall composition (tie line 23) the amount of the top phase is much smaller than that of the bottom phase. At the same time the equilibrium concentrations deviate only little from those in a system with a phase ratio near unity. Thus, the small amount of dextran in the top phase consists of the very short dextran molecules which are readily available due to the high overall dextran content of the system. Simultaneously the molecular-weight distri-


Figure 4. Molecular-weight distributions of dextran in the coexisting phases of tie lines $13(-), 23(--)$, and $27(\cdots)$.


Figure 5. (Top) Molecular-weight distributions of polydisperse PEG in the top phase of tie lines $13(-), 23(--)$, and 27 (...). (Bottom) Molecular-weight distributions of polydisperse PEG in the bottom phase of tie lines 13 (一), 23 ( -- ), and $27(\cdots)$.
bution of dextran in the top phase is narrow ( $M_{\mathrm{w}} / M_{\mathrm{n}}=1.74$ ), whereas the distribution in the bottom phase is essentially the same as that in the stock solution ( $M_{\mathrm{w}} / M_{\mathrm{n}}=4.32$ ).

If the overall concentration of PEG in the system is increased, more dextran has to dissolve in the increasing amount of the top phase to maintain the dextran concentration. The dextran molecules partitioning to the top phase now have to be of higher molecular weight since not enough short molecules are available. Thus, the molecular-weight distribution of dextran in the top phase broadens ( $M_{\mathrm{w}} / M_{\mathrm{n}}=$ 1.78 ) and is shifted to higher average values of molecular weight. Since the short dextran molecules are then missing in the bottom phase, the dextran molecular-weight distribution in the bottom phase becomes narrower ( $M_{w} / M_{n}=3.95$ ) and is also shifted to higher average values.
Exactly the same arguments hold for the distribution of PEG with different molecular weights between the phases. This can be seen in Figure 5 where the molecular-weight distributions of PEG in the top and bottom phases are shown again for the three tie lines 13, 23 (dextran rich), and 27 (PEG
rich). Preferably the short PEG molecules partition to the dextran-rich bottom phase. Thus, the average molecular weight of PEG in the bottom phase is low for a PEG-rich overall composition. Simultaneously the molecular-weight distribution of PEG in the top phase is essentially the same as in the stock solution. The average molecular weight of PEG in the bottom phase as well as in the top phase increases as the phase ratio is shifted toward a dextran-rich overall composition of the system.

Registry Numbers Supplied by Author. Poly(ethylene glycol), 25322-68-3; dextran, 9004-54-0.

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[^0]:    ${ }^{a} M_{\mathrm{n}}=$ number-average molecular weight; $M_{\mathrm{w}}=$ mass-average molecular weight.

